

New Paradigms for Topological Matter

Theory group of Tomáš Bzdušek

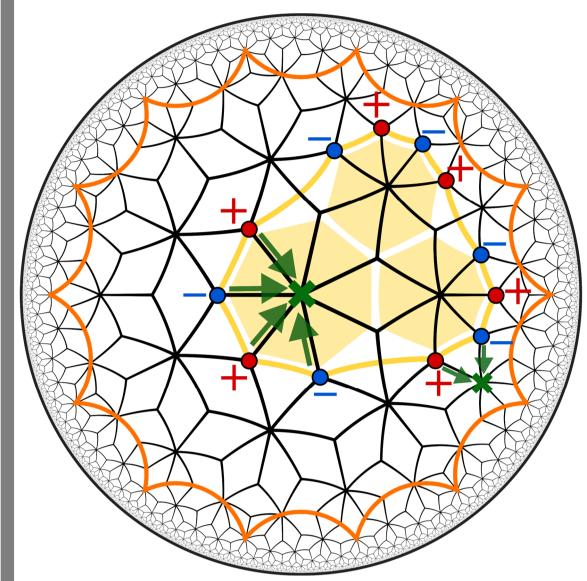
Patrick M. Lenggenhager and Tomáš Bzdušek



What we do

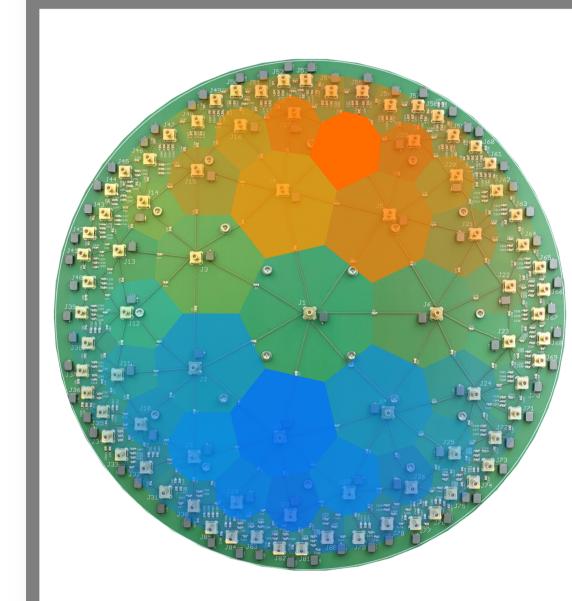
We study the mathematical characterization and physical manifestations of **topological phases of matter**. This includes topological aspects of electron energy bands in crystalline solids, notably in topological insulators, (semi)metals, and superconductors. In addition, we consider artificial (e.g. hyperbolic) lattices and also non-equlibrium (driven and dissipative) systems. The research group will fully launch in the fall of 2023, but we can already take on bachelor and master students!

Flat bands and correlations



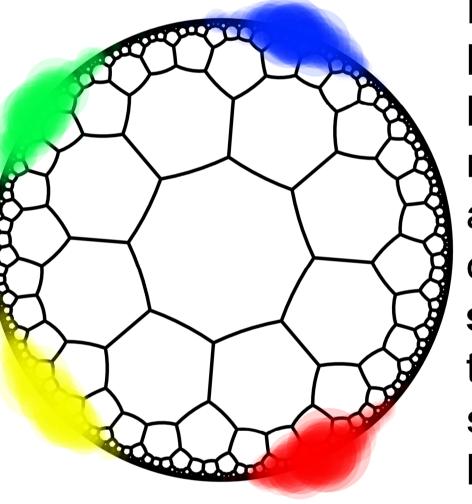
In models with dispersionless (flat) bands, the kinetic energy is small, and the physics is dominated by particle interactions. We aim to study correlated phases in hyperbolic lattices (with and without flat bands).

Artificial lattices (metamaterials)



Metamaterials (such as electric-circuit networks, or coupled photon resonators) allow for controlled experimental realizations of designed systems on arbitrary lattices. Even lattices in negatively curved space, which can't be realized with crystalline solids, can be emulated.

Hyperbolic topological insulators



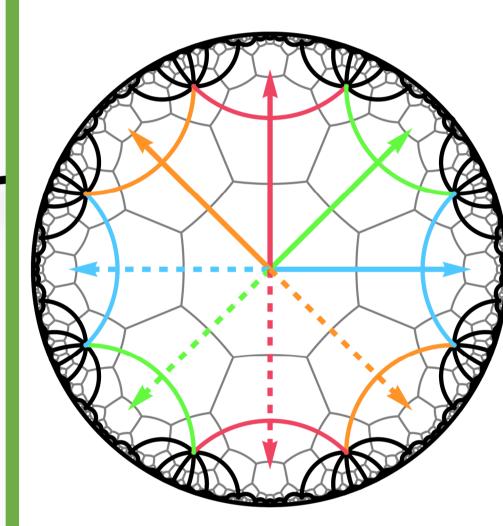
Hyperbolic lattices have an extensive boundary, which might be favorable for an efficient realization of topological edge states. Characterization of topological states with hyperbolic band theory is still an open problem.

insulators lattice symmetries

Hyperbolic

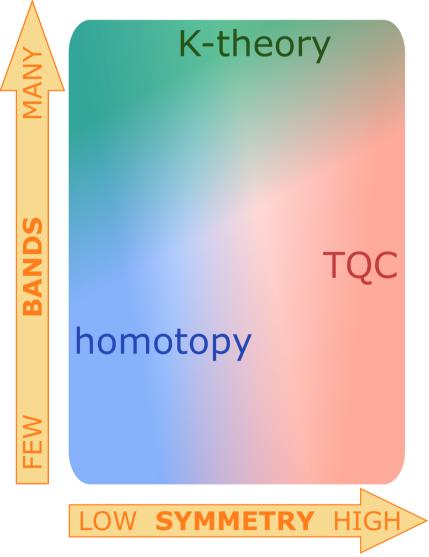
lattices

Translation symmetry



Translations in hyperbolic lattices do not commute. This has important consequences for the hyperbolic extension of the (Bloch) band theory; for example, the Brillouin zone becomes higherdimensional.

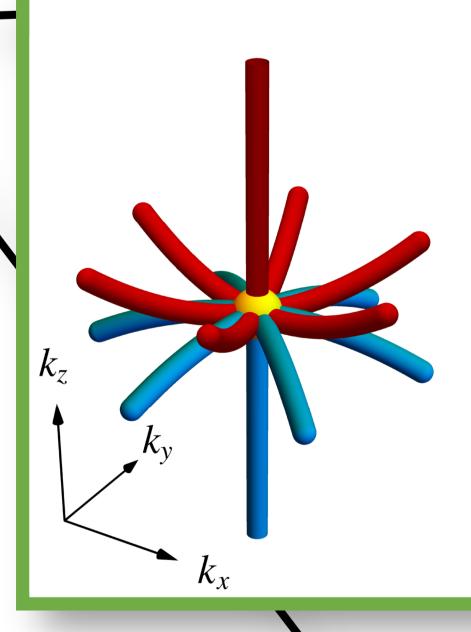
Classification of topological invariants



Depending on the symmetry and the available degrees of freedom, diverse mathematical techniques are useful for capturing topological features, coming in varying levels of robustness.

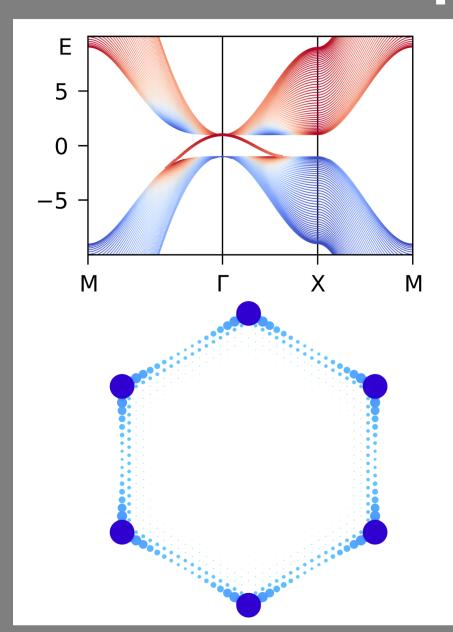
Topology Band nodes semimetals

Characterization of band nodes



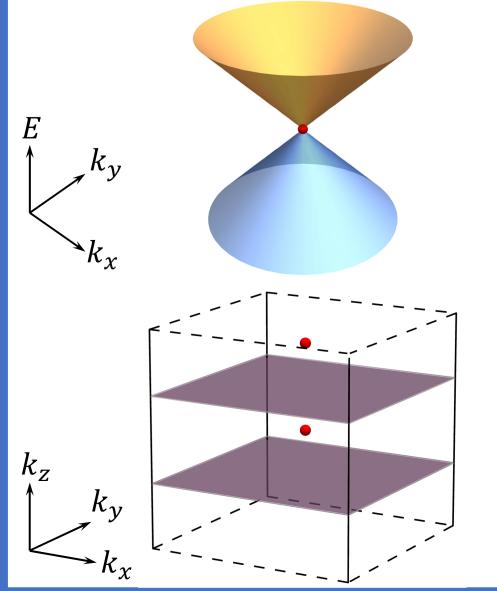
Symmetries do not only protect certain band nodes, but they also constrain the Hamiltonian in their vicinity. This allows us to predict and classify certain nodal features using symmetry.

Bulk boundary correspondence



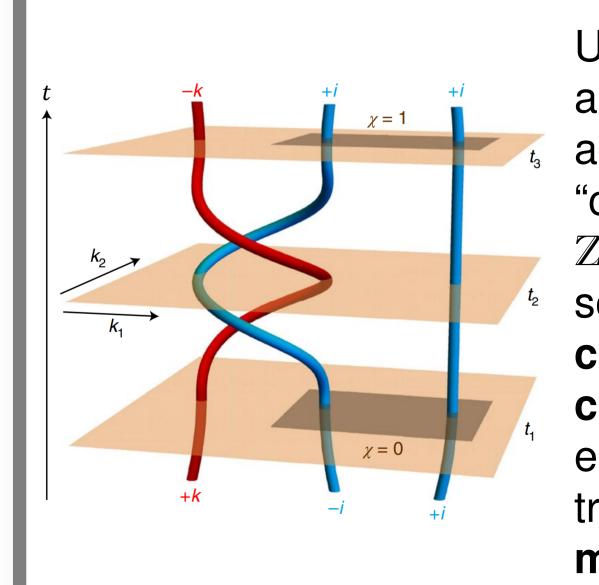
Non-trivial bulk topology in insulators and semimetals is reflected in their boundary signatures. Often, these are conducting states on the surface, but they can also be more intricate, such as a fractional electric charge accumulated at corners.

Topological semimetals



Band topology also plays a role in semi-metals, where it relates to degeneracies of energy bands, known as band nodes. These take the role of metallic (i.e. gap-closing) transitions separating slices of insulators in one fewer dimensions.

Non-Abelian braiding



Usually, band nodes are characterized by additive topological "charges" (such as \mathbb{Z} or \mathbb{Z}_2). However, sometimes, these charges are noncommutative, thus enabling their nontrivial braiding in momentum space.